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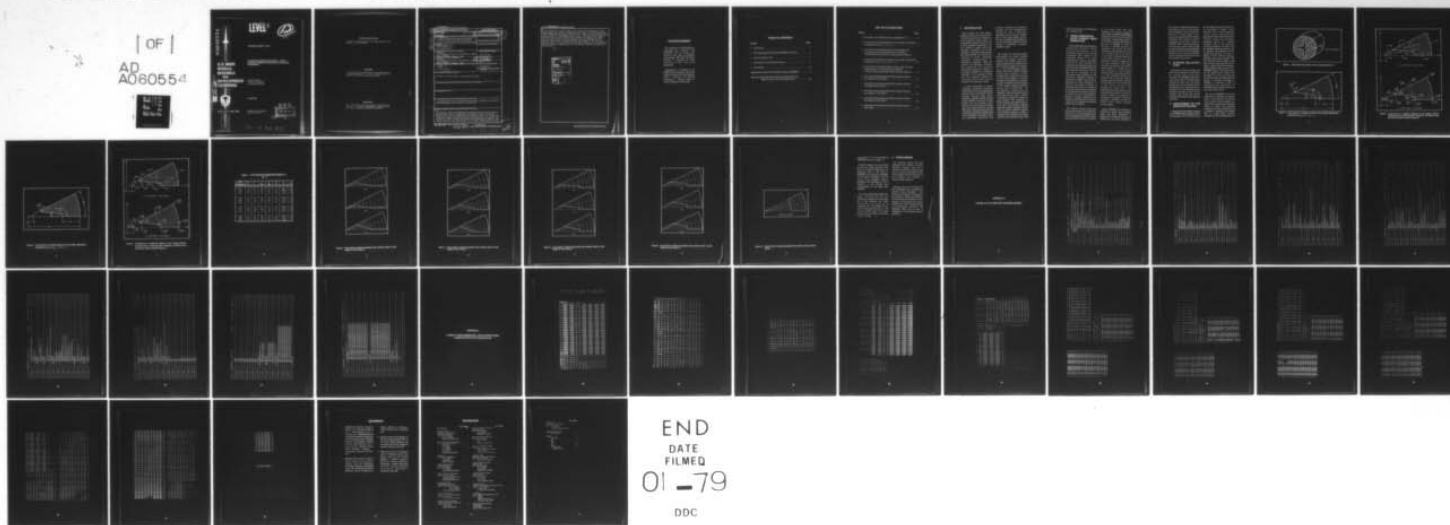
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A COUPLED INTERIOR BALLISTICS-FINITE ELEMENT COMBUSTION INSTABI--ETC(U)

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**U.S. ARMY
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Redstone Arsenal, Alabama 35809

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TECHNICAL REPORT T-78-72

**A COUPLED INTERIOR BALLISTICS — FINITE
ELEMENT COMBUSTION INSTABILITY ANALYSIS
PROCEDURE**

Robert M. Hackett
Propulsion Directorate
Technology Laboratory

14 July 1978

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20. ABSTRACT (Continue on reverse side if necessary and identify by block number)		
An executive routine is developed which should provide the solid propellant grain designer with the capability of performing an interior ballistics analysis while, with a minimum amount of additional effort, at the same time performing a combustion instability prediction analysis of the system. The routine, in effect, couples the output of an existing solid propellant grain design evaluation code, which predicts the acoustic chamber geometry during		

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surface regression, with the input to the existing three-dimensional finite element combustion instability prediction code, FLAP3. The three-dimensional finite element mesh and boundary conditions are generated from the grain surface regression data for the progressive burn times. The entire finite element mesh and boundary condition generation by FLESH3, the companion to FLAP3, is executed with the input of seven parameters, which are obtained from the ballistics code output or from the initial grain geometry. The use of the developed routine, in conjunction with the two existing codes, is demonstrated through a number of example cases of a star design, along with the case of a shell design.

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1. INTRODUCTION

Until recently the term Interior Ballistics referred to the computation of head end pressure and thrust in solid propellant rocket motors by quasi-steady analysis. However, with recently developed technology^{1,2}, it is now possible to predict, given the necessary propellant and nozzle admittance and response parameters, the linear stability of a rocket motor subjected to small, combustion amplified, disturbances, i.e., combustion instability. With the advent of low signature constraints, this capability has assumed considerable importance because of the high probability of combustion instability in low signature motors and the attendant jeopardy to successful motor (and system) operation that instability creates.

A major shortcoming of current combustion instability prediction technology is that it is computationally divorced from conventional interior ballistic analysis. This makes instability analysis difficult because interior ballistic data must be hand loaded into the stability codes. Moreover, it has fostered a functional split, with interior ballistic analysis the domain of the grain designer while combustion instability analysis is that of the "instability specialist". Due to the difficulties associated with

running combustion instability analyses and the aforementioned functional split, combustion instability has not been an integral part of the motor design process. Clearly, a successful motor design for any low signature application should include a combustion instability prediction aspect.

The remedy for this shortcoming would seem to be obvious: combine conventional interior ballistics analysis and stability codes into a single complete interior ballistics code that the motor designer can employ, i.e., a code that performs pressure, thrust, and linear stability margin versus time analyses virtually simultaneously. In this way, it is easy for the motor designer to consider combustion instability. It is with this concept in mind that the development of the computer program described herein was undertaken. Its development is based upon the utilization of the previously developed three-dimensional finite element combustion instability prediction code, FLAP3². The utilization of FLAP3 requires automatic finite element mesh and boundary condition generation, and the coupling of FLAP3 with an interior ballistics analysis code, therefore, requires, in effect, a coupling of the ballistics code output with the mesh generator input. This

process is the essence of a development of a combined code.

2. THREE-DIMENSIONAL FINITE ELEMENT MESH GENERATION

FLAP3 (Fluid Analysis Program, 3 Dimensions) performs a linear acousto-modal analysis of the irrotational motions of an inviscid, compressible fluid coupled to the irrotational motions of a nearly incompressible, linearly viscoelastic solid, and a linear potential flow analysis of the irrotational motions of an inviscid, incompressible fluid, and then determines the effect of the flow field and of combustion on the calculated acoustic oscillations^{2,3}. This combustion instability analysis is performed at different points in time, beginning at initial combustion, or time zero. The output of FLAP3 is modal frequency and an evaluation of the pressure growth/decay coefficient α for each mode of vibration analyzed. A positive net value of α indicates a growth of pressure oscillations and, therefore, instability while a negative value of α is an indication of decaying oscillations, or stability.

The FLAP3 analysis utilizes the finite element method and models the acoustic cavity and propellant grain as an assemblage of three-dimensional quasi-hexahedral elements connected

at the corner nodes. The mesh generation code used in conjunction with FLAP3 is FLESH3 (Fluid Mesh, 3 Dimensions) which was developed for the purpose of generating input data for FLAP3. A detailed description of the use of FLESH3 is found in *Reference 3*. FLESH3 generates the numbered nodal points and nodal coordinates and identifies each node as to whether it lies in the acoustic cavity, on the cavity-grain interface, or in the grain; generates the quasi-hexahedral elements, designated by the eight numbered nodal points defining each element, and identifies each element as to whether it is a cavity element, a cavity element adjacent to the cavity-grain interface, or a solid propellant element; and generates the cavity-grain interface element surfaces (burning surfaces) and identifies each as to the direction of the surface normal. This information, along with a few additional input data relative to gas and propellant properties and type of acoustic mode(s) to be analyzed, is necessary and sufficient to activate a combustion instability analysis by FLAP3, given adequate computational facilities.

Input to FLESH3 is in the form of a definition of global curves, defining cavity and grain boundaries; a designation of blocks of points, as to whether they are cavity, interface or

grain points; a designation of blocks to be generated, by their nodal indices; and a designation of the number and location of longitudinal cross-sections, defining the number of layers of elements. The objective is that of minimizing the amount of input to FLESH3. This can be done by the use of an executive routine which accepts as input a small number of geometrical parameters from the interior ballistics code and, in turn, activates FLESH3. The development of this routine is the major thrust of this report.

3. INTERIOR BALLISTICS CODE

The interior ballistics analysis code used in the formulation was developed by Aerojet Solid Propulsion Company⁴. The FLESH3 geometrical input parameters are, therefore, those presented in that code, but similar parameters would be obtained from a consideration of a comparable interior ballistics code. The description of the developed executive routine will be related to the Aerojet code, but the procedure followed in the development is general.

4. DEVELOPMENT OF THE EXECUTIVE ROUTINE

A listing of the formulated computer code GRNMSH (Grain Mesh) is found in Appendix A. The code is based upon

the star design found in *Reference 4* and reproduced in *Figure 1*. One computer card of input parameters (seven values) automatically generates the three-dimensional finite element mesh and boundary conditions needed for a FLAP3 analysis. Due to the dihedral symmetry provision in FLAP3, only the smallest repeating segment need be analyzed. This segment, for the general star geometry, is shown in *Figures 2 and 4*; with the necessary geometry parameters identified. The only difference between *Figure 2* and *Figure 4* is that the angle Φ is zero in *Figure 4*. This condition necessitated a slightly different internal provision in GRNMSH. *Figures 3 and 5* indicate: (a) the key global curves (others were generated, as can be seen from the included example), and (b) the key part indices. A working knowledge of FLESH3³ is necessary in order to understand the intricacies of GRNMSH, and to modify and add to it, but not in order to use it.

The use of GRNMSH can best be understood by following an example. *Table 1*, from *Reference 4*, lists the twelve cases of the star design upon which the formulation of the executive routine is based. The generated meshes for the twelve cases are shown in *Figures 6 through 9*. The special case of a shell design (circular cylinder), for which the parameter Φ is

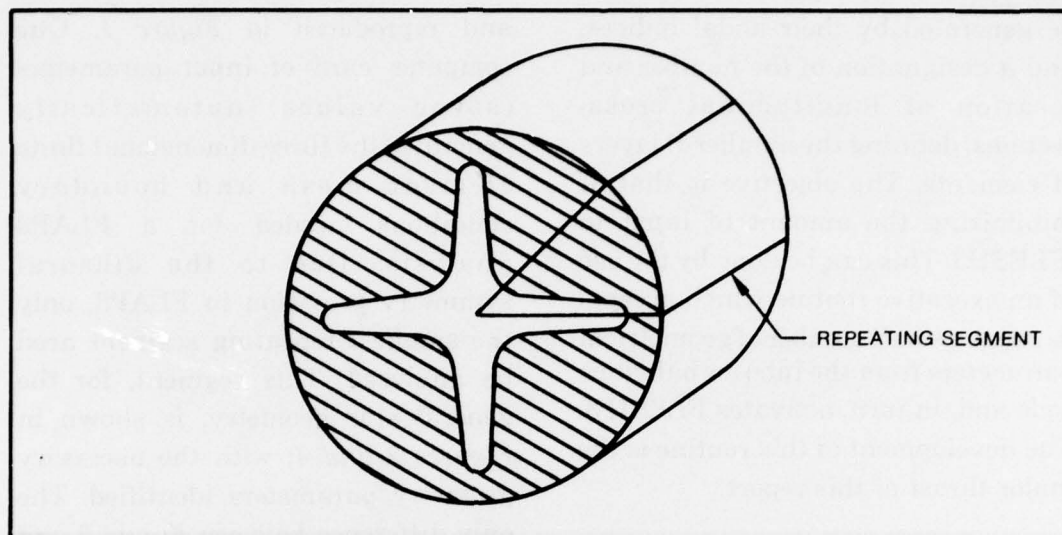


Figure 1. Star design with outside round on propellant tip; $N=4$

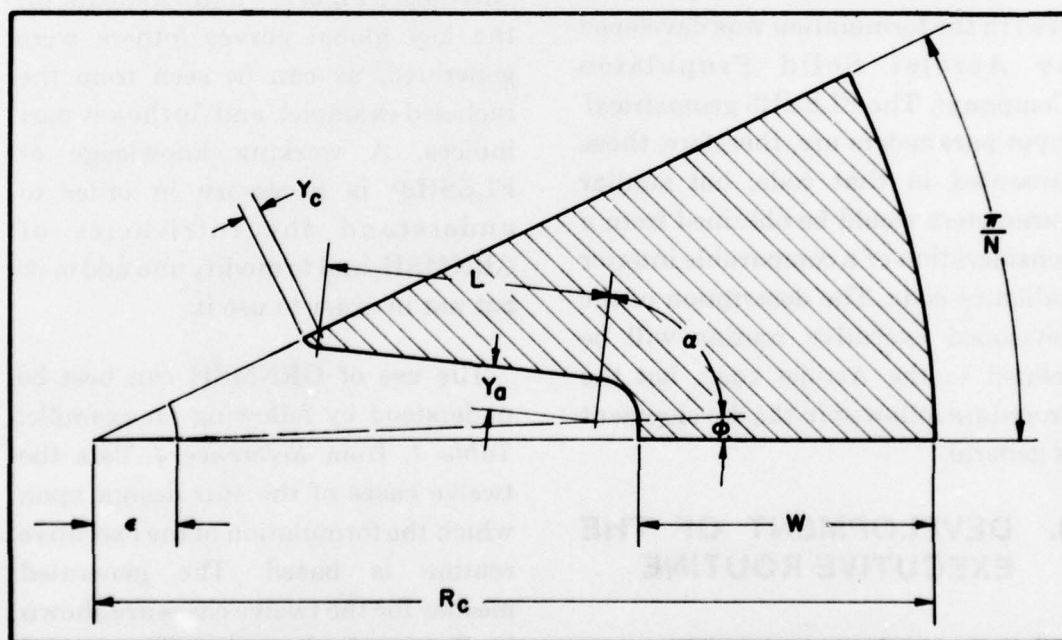


Figure 2. Cross-section of repeating segment of star design; independent parameters: $N, R_c, w, \phi, Y_a, \alpha, L$

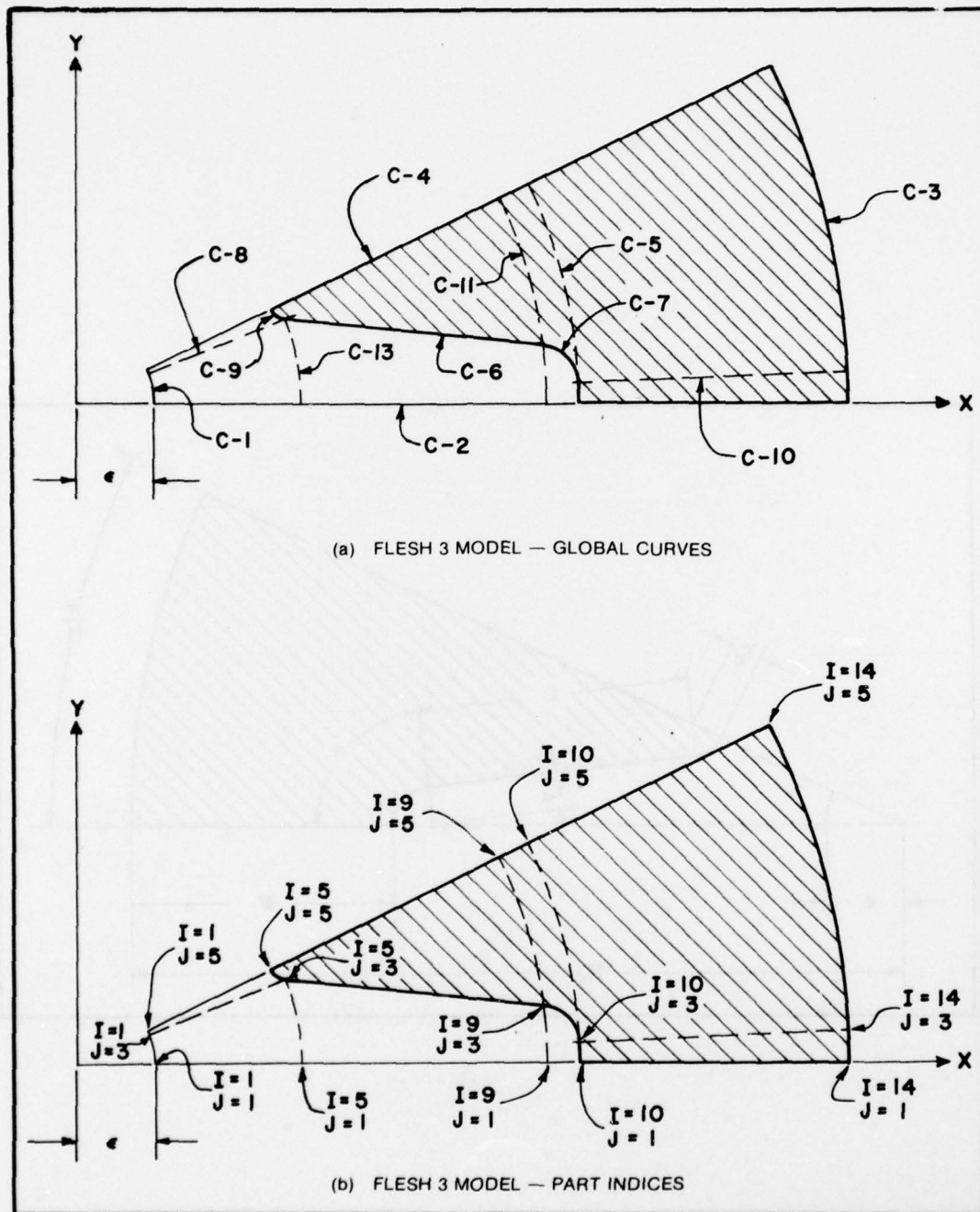


Figure 3. Cross-section of repeating segment of star design showing important input to mesh generator (FLESH 3): (a) Global curves and (b) Part indices (matches Figure 2).

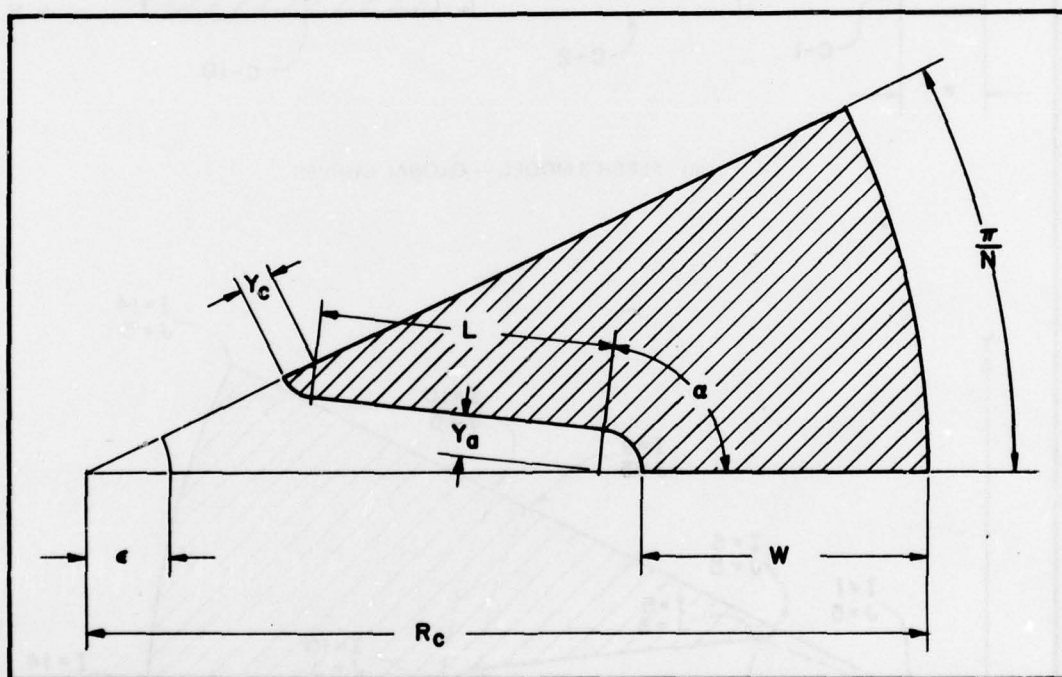


Figure 4. Cross-section of repeating segment of star design; independent parameters: N , R_c , w , Y_a , α , L ; $\Phi = 0$

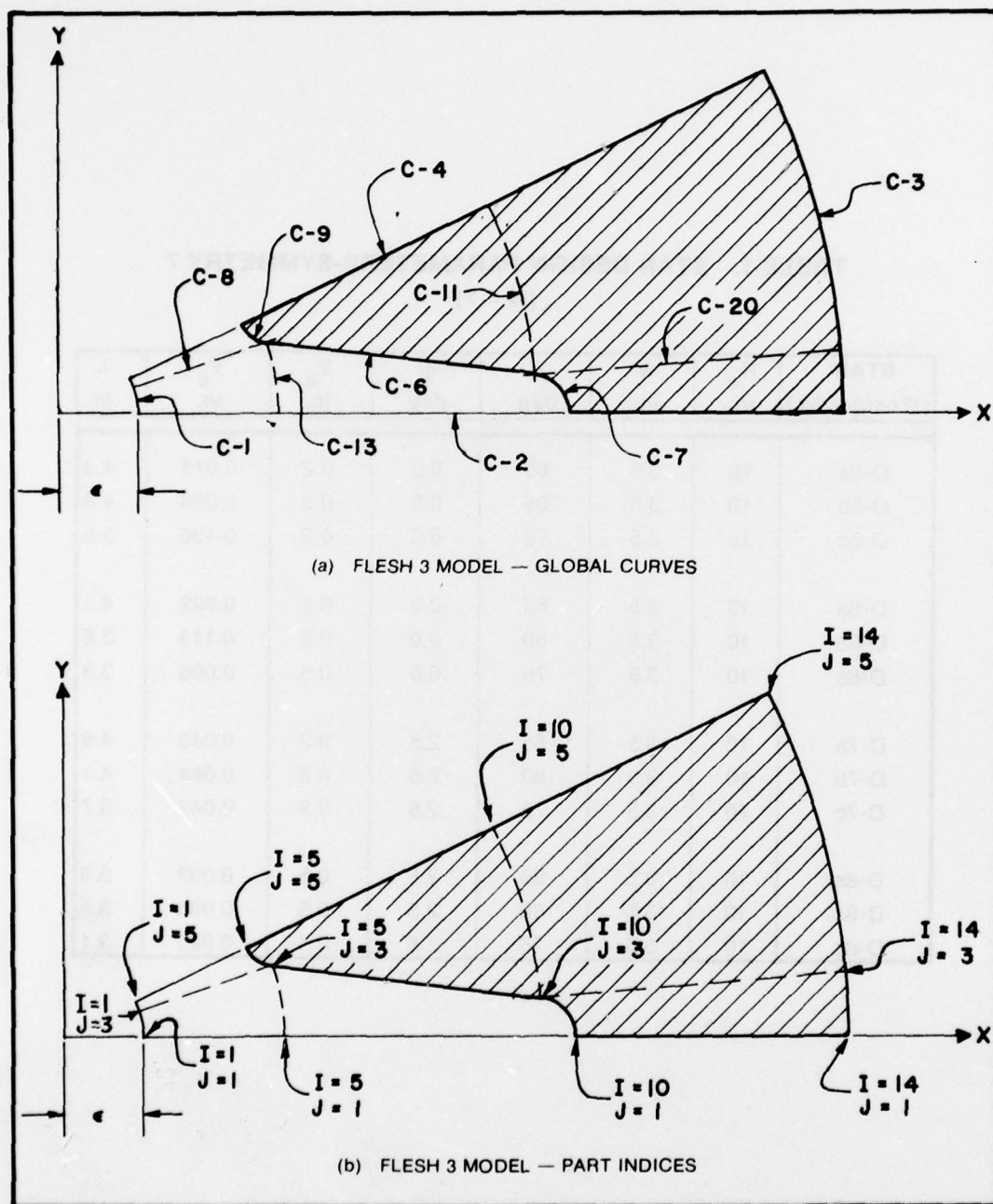


Figure 5. Cross-section of repeating segment of star design showing important input to mesh generator (FLESH3): (a) Global curves and (b) Part indices (matches Figure 4).

TABLE 1. STAR DESIGN PARAMETERS-SYMMETRY 7
(N = 7)

STAR (Design No.)	R _c in.	w in.	α deg	Φ deg	Y _a in.	Y _c in.	L in.
D-5a	10	3.5	80	0.0	0.2	0.075	4.3
D-5b	10	3.5	85	0.0	0.2	0.068	4.9
D-5c	10	3.5	75	0.0	0.2	0.136	3.8
D-6a	10	3.5	85	0.0	0.5	0.092	4.1
D-6b	10	3.5	80	0.0	0.5	0.118	3.6
D-6c	10	3.5	75	0.0	0.5	0.095	3.3
D-7a	10	3.5	85	2.5	0.2	0.043	4.8
D-7b	10	3.5	80	2.5	0.2	0.084	4.1
D-7c	10	3.5	75	2.5	0.2	0.047	3.7
D-8a	10	3.5	85	2.5	0.5	0.092	3.9
D-8b	10	3.5	80	2.5	0.5	0.035	3.5
D-8c	10	3.5	75	2.5	0.5	0.069	3.1

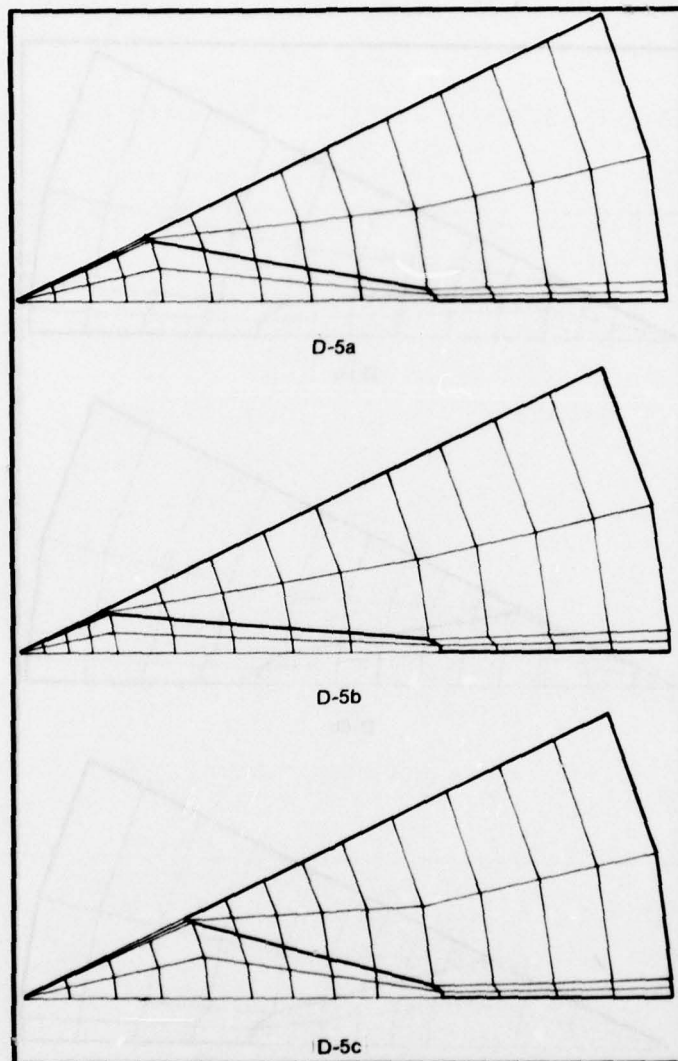


Figure 6. Cross-section showing generated finite element mesh for star design D-5 (see Table 1).

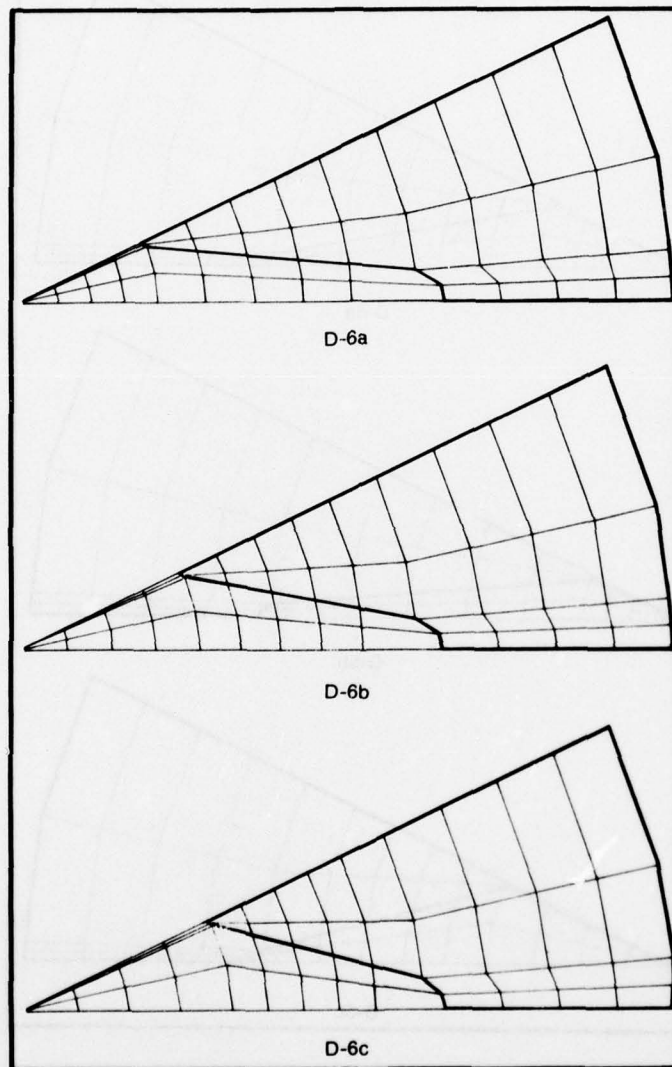


Figure 7. Cross-section showing generated finite element mesh for star design D-6 (see Table 1).

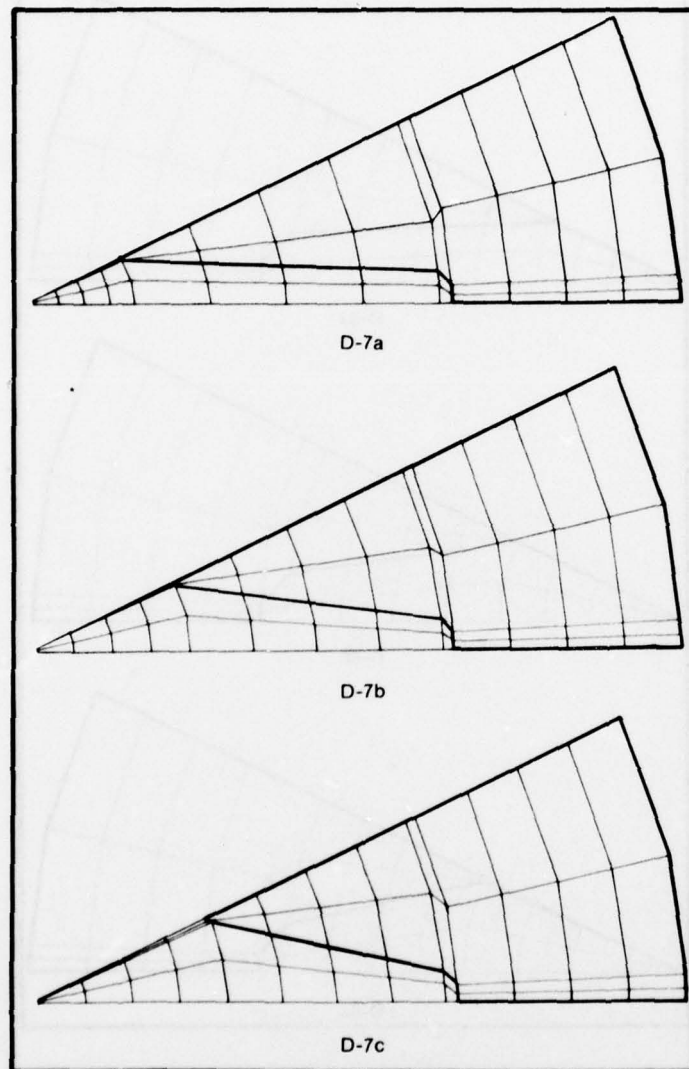


Figure 8. Cross-section showing generated finite element mesh for star design D-7 (see Table 1).

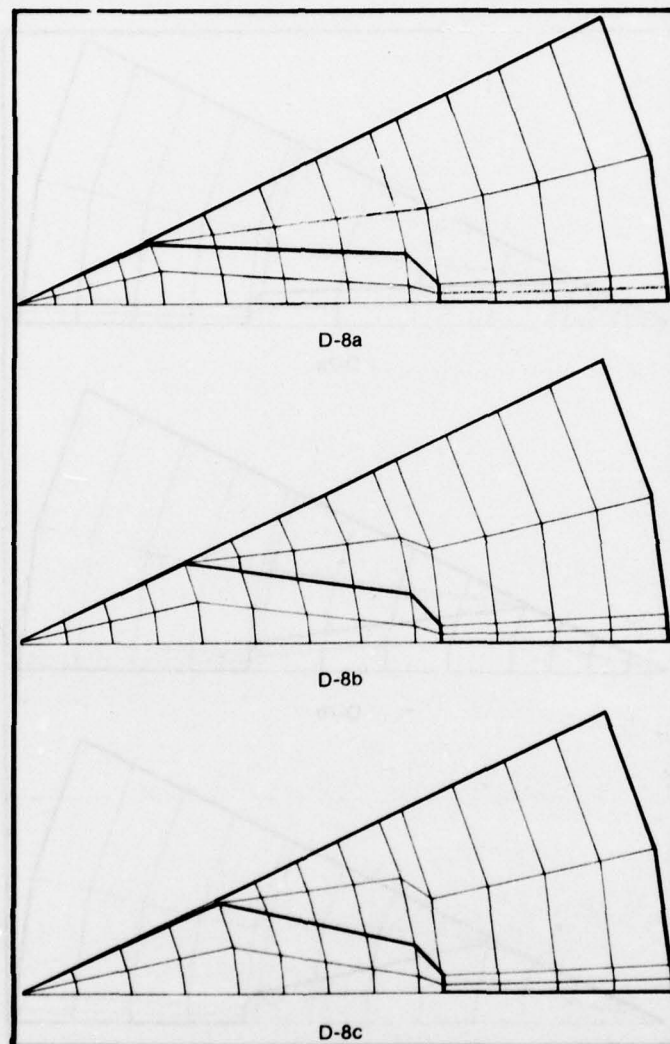


Figure 9. Cross-section showing generated finite element mesh for star design D-8 (see Table 1).

CONCLUSIONS

An extensive program has been developed which couples an interior shell stress analysis with a component flexibility analysis. This is useful for the design of pressure vessels and the prediction of their behavior under various loading conditions.

Basically, the goal of this program is to provide a means for the analysis of the behavior of a shell structure under various loading conditions. The program is able to handle a wide range of loading conditions and can be used for the design of pressure vessels and the prediction of their behavior under various loading conditions.

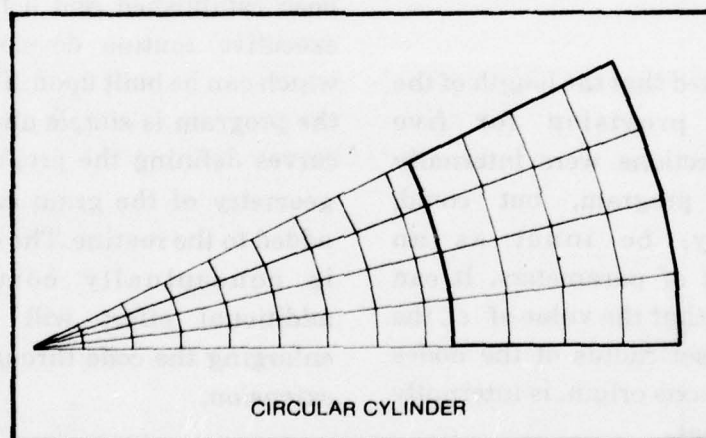


Figure 10. Cross-section showing generated finite element mesh for shell design.

input equal to π/N , as generated by GRNMSH is shown in *Figure 10*.

Sample computer input and output for the star design geometry D-5a (*Table 1*) is found in Appendix B. In sequential order is: the input to GRNMSH, the output from GRNMSH (or the input to FLESH 3), and the output from FLESH3. Again, familiarity with FLESH3, by way of *Reference 3*, will enhance one's understanding of the output from FLESH3.

It can be noted that the length of the grain, and provision for five equidistant sections were internally set in the program, but could, alternatively, be input as an additional set of parameters. It can also be noted that the value of ϵ , the necessary offset radius of the nodes closest to the axis origin, is internally set at 0.1 inches.

5. CONCLUSIONS

An executive routine has been developed which couples an interior ballistics analysis code with a combustion instability analysis code; thus, in concept, providing the rocket motor designer with the potential for a more inclusive and, therefore, a superior design approach.

Basically, the proof of concept has been established and a fundamental executive routine developed — one which can be built upon. The format of the program is simple and additional curves defining the progressive burn geometry of the grain can be easily added to the routine. The development is conceptually complete; the additional effort will be that of enlarging the code through repetitive extension.

APPENDIX A

LISTING OF THE COMPUTER PROGRAM GRNMSH

PROGRAM	NAME	7-74	OPT=1	FTV 4.0-0.59	06/14/78	1-000.04	PAGE	3
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992	993	994	995	996	997	998	999	1000

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      NC(1)=15
      NP(1)=1.75
      175      AA(1)=SQON*(AA(19)-AA(1))*0.75
      NC(1)=AA(1)
      TM(1)=1.75
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      I=23
      180      GG=AA(16)*S-1-AC(7)*SIN(PH1*0.5)
      HH=AA(7)*COS(PH1*0.5)-AA(1)*CPH1
      SLOPE=GG/HH
      X(1)=AA(16)*CPH1-0.1
      Y(1)=AA(16)*SPH1+0.1*SLOPE
      185      I=24
      X(1)=AA(7)*COS(PH1*0.5)+0.1
      Y(1)=AA(7)*SIN(PH1*0.5)-0.1*SLOPE
      NC(1)=15
      217      CONTINUE
      I=25
      NC(1)=17
      NP(1)=1.75
      AA(1)=AA(19)*(AA(19)-AA(19))*0.75
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      TM(1)=1.75
      218      CONTINUE
      I=27
      X(1)=SC
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      NC(1)=15
      219      CONTINUE
      220      CONTINUE
      I=28
      WV=RC*(YA*SIN(ALPHA)/(RC-YA+YA)*COS(ALPHA))-CYA*SPH1+YA*SFAP
      225      WV=RC*CYA*CPH1+YA*CFAP
      SLOPE=WV/X
      X(1)=RC*YA*CPH1+YA*CFAP-0.1
      Y(1)=RC*YA*SPH1+YA*SFAP-0.1*SLOPE
      I=29
      X(1)=SC
      Y(1)=RC*(YA*CTN(ALPHA)/(RC-YA+YA)*COS(ALPHA))
      NC(1)=20
      221      CONTINUE
      222      CONTINUE
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      I=33
      WV=AA(16)*S-1-AC(7)*SIN(PH1*0.5)
      HH=AA(7)*COS(PH1*0.5)-AA(1)*CPH1
      SLOPE=WV/HH
      X(1)=AA(16)*CPH1-0.1
      Y(1)=AA(16)*SPH1+0.1*SLOPE

```


PROGRAM	GNASH	74/74	OPT=1	FTD	4000000	PAGE	4
235	CONTINUE						
236	CONTINUE						
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398	CONTINUE						
399	CONTINUE						
400	CONTINUE						

PROGRAM GRNWSH	74/74	OPT=1	FTN 4.6439	06/14/78 13.09.04	PAGE 7
345	345				
350	350				
355	355				
360	360				
365	365				
370	370				
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380	380				
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845	845				
850	850				
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870	870				
875	875				
880	880				
885	885				
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935	935				
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950	950				
955	955				
960	960				
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970	970				
975	975				
980	980				
985	985				
990	990				
995	995				

25

APPENDIX B

EXAMPLE THREE-DIMENSIONAL FINITE ELEMENT MESH GENERATION FOR STAR DESIGN (D-5A)

7.0	10.0	3.5	0.0	0.2	80.0	4.3
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GRAIN MESH									
14	5	29	7	1.00	5				
0.0000	0.0000	1	25	.1000	.1000	0.0000	25.7143		
0.0000	0.0000	0	0	0.0000	0.0000	0.0000	0.0000		
10.0000	0.0000	2	0	0.0000	0.0000	0.0000	0.0000		
0.0000	0.0000	1	25	10.0000	10.0000	0.0000	25.7143		
0.0000	0.0000	0	0	0.0000	0.0000	0.0000	0.0000		
10.0000	0.0000	4	0	0.0000	0.0000	0.0000	0.0000		
0.0000	0.0000	5	25	6.5000	6.5000	0.0000	25.7143		
2.0000	.9613	0	0	0.0000	0.0000	0.0000	0.0000		
6.4347	.1793	6	0	0.0000	0.0000	0.0000	0.0000		
0.0000	0.0000	7	50	.2000	.2000	0.0000	25.7143		
0.0000	0.0000	0	0	0.0000	0.0000	0.0000	0.0000		
2.2001	.9886	8	0	0.0000	0.0000	0.0000	0.0000		
2.1131	1.0176	9	54	.0751	.0751	204.7143	251.0000		
0.0000	0.0000	0	0	0.0000	0.0000	0.0000	0.0000		
10.0000	0.0000	10	0	0.0000	0.0000	0.0000	0.0000		
0.0000	0.0000	11	25	6.3378	6.3378	0.0000	25.7143		
0.0000	0.0000	0	0	0.0000	0.0000	0.0000	0.0000		
10.0000	2.2824	12	0	0.0000	0.0000	0.0000	0.0000		
0.0000	0.0000	13	25	2.3023	2.3023	0.0000	25.7143		
2.1886	.5248	0	0	0.0000	0.0000	0.0000	0.0000		
6.4378	-.0125	14	0	0.0000	0.0000	0.0000	0.0000		
0.0000	0.0000	15	25	1.7517	1.7517	0.0000	25.7143		
6.2378	0.0000	0	0	0.0000	0.0000	0.0000	0.0000		
6.6880	0.0000	16	0	0.0000	0.0000	0.0000	0.0000		
0.0000	0.0000	17	25	5.3289	5.3289	0.0000	25.7143		
0.0000	0.0000	0	0	0.0000	0.0000	0.0000	0.0000		
10.0000	0.0000	18	0	0.0000	0.0000	0.0000	0.0000		
6.2347	.1834	0	0	0.0000	0.0000	0.0000	0.0000		
10.0000	.3109	20	0	0.0000	0.0000	0.0000	0.0000		
0.0000	0.0000	0	0	0.0000	0.0000	0.0000	0.0000		
10.0000	.1555	22	0	0.0000	0.0000	0.0000	0.0000		
2.1886	.5221	0	0	0.0000	0.0000	0.0000	0.0000		
6.5728	.0909	24	0	0.0000	0.0000	0.0000	0.0000		
0.0000	0.0000	0	0	0.0000	0.0000	0.0000	0.0000		
2.1822	.9947	26	0	0.0000	0.0000	0.0000	0.0000		
1.9822	.9379	0	0	0.0000	0.0000	0.0000	0.0000		
6.3378	1.4286	28	0	0.0000	0.0000	0.0000	0.0000		
6.0788	1.3882	0	0	0.0000	0.0000	0.0000	0.0000		
6.4370	1.4689	30	0	0.0000	0.0000	0.0000	0.0000		
2.5080	.5706	0	0	0.0000	0.0000	0.0000	0.0000		
10.0000	2.2824	32	0	0.0000	0.0000	0.0000	0.0000		
0.0000	0.0000	0	0	0.0000	0.0000	0.0000	0.0000		
10.0000	1.1267	34	0	0.0000	0.0000	0.0000	0.0000		
0.0000	0.0000	0	0	0.0000	0.0000	0.0000	0.0000		
10.0000	2.2824	36	0	0.0000	0.0000	0.0000	0.0000		
0.0000	0.0000	0	0	0.0000	0.0000	0.0000	0.0000		
10.0000	5.4992	38	0	0.0000	0.0000	0.0000	0.0000		
1.9822	.9379	0	0	0.0000	0.0000	0.0000	0.0000		
6.2709	1.4215	40	0	0.0000	0.0000	0.0000	0.0000		
1	1	1	4	5					
1	5	1	9	2					
2	5	3	5	5					
2	6	3	9	5					
3	18	1	10	4					
3	6	4	14	5					
3	11	1	14	1					
3	1	1	5	2	2	13	12	1	1
3	1	2	5	3	12	13	8	1	1
3	1	3	4	4	8	15	26	1	1
3	1	4	4	5	26	15	8	1	1
3	5	1	9	2	2	17	24	13	1
3	4	3	5	4	4	26	15	2	0

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9	9	1	10	2	2	7	24	17	2	0	0	0	0
10	3	2	10	3	24	7	6	17	2	0	0	0	0
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2.0000													
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2	1	2	5	3	12	13	8	1	1	0	0	0	0
3	1	3	4	4	8	15	26	1	1	0	0	0	0
4	1	4	4	5	26	15	4	1	1	0	0	0	0
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6	4	3	5	4	8	9	26	15	2	0	0	0	0
7	4	4	5	5	26	9	4	15	2	0	0	0	0
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16	10	2	14	3	22	3	20	7	3	0	0	0	0
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2.0000													
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3	1	3	4	4	8	15	26	1	1	0	0	0	0
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6	4	3	5	4	8	9	26	15	2	0	0	0	0
7	4	4	5	5	26	9	4	15	2	0	0	0	0
8	5	2	9	3	24	17	6	13	2	0	0	0	0
9	9	1	10	2	2	7	24	17	2	0	0	0	0
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2.0000													
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3	1	3	4	4	8	15	26	1	1	0	0	0	0
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2.0000													
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11	5	3	9	4	6	17	40	9	3	0	0	0	0
12	5	4	9	5	40	17	4	9	3	0	0	0	0

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15	10	1	14	2	2	3	22	7	3	0	0	0	0	0
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17	10	3	14	4	20	3	32	11	3	0	0	0	0	0
18	10	4	14	5	32	3	4	11	3	0	0	0	0	0
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6.0000														
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3	1	3	4	4	8	15	26	1	1	0	0	0	0	0
4	1	4	4	5	26	15	4	1	1	0	0	0	0	0
5	1	5	9	2	2	17	24	13	1	0	0	0	0	0
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12	5	4	9	5	40	17	4	9	3	0	0	0	0	0
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15	10	1	14	2	2	3	22	7	3	0	0	0	0	0
16	10	2	14	3	22	3	20	7	3	0	0	0	0	0
17	10	3	14	4	20	3	32	11	3	0	0	0	0	0
18	10	4	14	5	32	3	4	11	3	0	0	0	0	0
-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
6.0000														
END														

CARD I. TITLE.

GRIN WESH

CARD II. CONTROL.

INX JMAX NNC I2C SCALE NLAY

14 5 34 7 1.

CARD III. PART BOUNDARY CURVE.

X - COORD	Y - COORD	MN	NP	A X-AXIS	B Y-AXIS	THETA1	THETA2
0.000	0.000	1	25	.10000	.10000	0.00000	25.71430
0.000	0.000	0	0	0.00000	0.00000	0.00000	0.00000
10.000	0.000	2	0	0.00000	0.00000	0.00000	0.00000
0.000	0.000	4	25	10.00000	10.00000	0.00000	25.71430
0.000	0.000	0	0	0.00000	0.00000	0.00000	0.00000
10.000	4.416	4	0	0.00000	0.00000	0.00000	0.00000
0.000	0.000	5	25	6.50000	6.50000	0.00000	25.71430
0.000	.461	0	0	0.00000	0.00000	0.00000	0.00000
6.435	.179	6	0	0.00000	0.00000	0.00000	0.00000
6.300	0.000	7	20	.20000	.20000	0.00000	20.00000
0.000	0.000	0	0	0.00000	0.00000	0.00000	0.00000
2.200	.444	8	0	0.00000	0.00000	0.00000	0.00000
2.111	1.012	9	54	.07510	.07510	204.71430	261.00000
0.000	0.000	0	0	0.00000	0.00000	0.00000	0.00000
10.000	0.000	10	0	0.00000	0.00000	0.00000	0.00000
0.000	0.000	11	25	6.33740	6.33740	0.00000	25.71430
0.000	0.000	7	0	0.00000	0.00000	0.00000	0.00000
10.000	2.242	12	0	0.00000	0.00000	0.00000	0.00000
0.000	0.000	13	25	2.30230	2.30230	0.00000	25.71430
2.145	.525	0	0	0.00000	0.00000	0.00000	0.00000
6.434	-.013	14	0	0.00000	0.00000	0.00000	0.00000
0.000	0.000	15	25	1.75170	1.75170	0.00000	25.71430
6.238	0.000	0	0	0.00000	0.00000	0.00000	0.00000
6.600	0.000	16	0	0.00000	0.00000	0.00000	0.00000
0.000	0.000	17	25	5.32890	5.32890	0.00000	25.71430
0.000	0.000	0	0	0.00000	0.00000	0.00000	0.00000
10.000	0.000	18	0	0.00000	0.00000	0.00000	0.00000
6.235	.183	0	0	0.00000	0.00000	0.00000	0.00000
10.000	.111	20	0	0.00000	0.00000	0.00000	0.00000
0.000	0.000	0	0	0.00000	0.00000	0.00000	0.00000
10.000	.156	22	0	0.00000	0.00000	0.00000	0.00000
2.145	.422	0	0	0.00000	0.00000	0.00000	0.00000
6.573	.091	24	0	0.00000	0.00000	0.00000	0.00000
0.000	0.000	0	0	0.00000	0.00000	0.00000	0.00000
2.182	.295	26	0	0.00000	0.00000	0.00000	0.00000
1.782	.738	0	0	0.00000	0.00000	0.00000	0.00000
6.338	1.429	28	0	0.00000	0.00000	0.00000	0.00000
6.079	1.188	0	0	0.00000	0.00000	0.00000	0.00000
6.437	1.469	30	0	0.00000	0.00000	0.00000	0.00000
2.500	.571	0	0	0.00000	0.00000	0.00000	0.00000
10.000	2.282	32	0	0.00000	0.00000	0.00000	0.00000
0.000	0.000	0	0	0.00000	0.00000	0.00000	0.00000
10.000	1.127	34	0	0.00000	0.00000	0.00000	0.00000
0.000	0.000	0	0	0.00000	0.00000	0.00000	0.00000
10.000	2.282	36	0	0.00000	0.00000	0.00000	0.00000
0.000	0.000	0	0	0.00000	0.00000	0.00000	0.00000
10.000	3.499	38	0	0.00000	0.00000	0.00000	0.00000
1.982	.738	0	0	0.00000	0.00000	0.00000	0.00000
6.279	1.422	40	0	0.00000	0.00000	0.00000	0.00000

CARD IV. NODE CODE SEQUENCE.

IC	I1	J1	I2	J2
1	1	1	4	5
1	5	1	9	2
2	5	1	5	5
2	5	3	6	4
1	10	1	10	1
1	6	4	14	5
1	11	1	14	3

CARD V. PART DEFINITION.

NP	T1	J1	T2	J2	L1	L2	L3	L4	MT	NH	I3	J3	IN
1	1	1	5	2	2	13	12	1	1	0	0	0	0
2	1	2	5	3	12	13	8	1	1	0	0	0	0
3	1	3	4	4	8	15	26	1	1	0	0	0	0
4	1	4	4	5	26	15	4	1	1	0	0	0	0
5	5	1	9	2	2	17	24	13	1	0	0	0	0
6	4	3	5	4	8	9	26	15	2	0	0	0	0
7	4	4	5	5	26	9	4	15	2	0	0	0	0
8	5	2	9	3	24	17	6	13	2	0	0	0	0
9	9	1	10	2	2	7	24	17	2	0	0	0	0
10	9	2	10	3	24	7	6	17	2	0	0	0	0
11	5	3	9	4	6	17	40	9	3	0	0	0	0
12	5	4	9	5	40	17	4	9	3	0	0	0	0
13	9	3	10	4	6	11	40	17	3	0	0	0	0
14	9	4	10	5	40	11	4	17	3	0	0	0	0
15	10	1	14	2	2	3	22	7	3	0	0	0	0
16	10	2	14	3	22	3	20	7	3	0	0	0	0
17	10	3	14	4	20	3	32	11	3	0	0	0	0
18	10	4	14	5	32	3	4	11	3	0	0	0	0
-1	0	0	0	0	0	0	0	0	0	0	0	0	0

CARD VI. SECTION LOCATION.

Z = 0.000

0.000

	X	Y	Z	WT
1	.10000	0.00000	0.00000	1
2	.65057	0.00000	0.00000	1
3	1.20115	0.00000	0.00000	1
4	1.75173	0.00000	0.00000	1
5	2.30230	0.00000	0.00000	1
6	5.05875	0.00000	0.00000	1
7	3.81560	0.00000	0.00000	1
8	4.57225	0.00000	0.00000	1
9	5.32850	0.00000	0.00000	1
10	6.50000	0.00000	0.00000	2
11	7.37500	0.00000	0.00000	3
12	8.25000	0.00000	0.00000	3
13	9.12500	0.00000	0.00000	3
14	10.00000	0.00000	0.00000	3
15	.09742	.02225	0.00000	1
16	.63424	.14476	0.00000	1
17	1.17029	.26727	0.00000	1
18	1.70774	.38977	0.00000	1
19	2.24447	.51248	0.00000	1
20	3.01448	.63739	0.00000	1
21	3.78449	.76241	0.00000	1
22	4.55450	.88743	0.00000	1
23	5.32452	.21245	0.00000	1
24	6.47242	.10065	0.00000	2
25	7.35427	.11436	0.00000	3
26	8.23572	.12807	0.00000	3
27	9.11716	.14177	0.00000	3
28	9.99860	.15548	0.00000	3
29	.09121	.04098	0.00000	1
30	.59340	.26664	0.00000	1
31	1.09558	.40229	0.00000	1

32	1.50776	.71193	0.00000	1
33	2.80802	.84881	0.00000	2
34	2.98392	.80952	0.00000	2
35	3.78773	.86817	0.00000	2
36	4.51166	.51841	0.00000	2
37	5.31352	.37666	0.00000	2
38	6.33681	.18679	0.00000	2
39	7.25234	.21788	0.00000	3
40	8.16691	.28883	0.00000	3
41	9.08088	.27978	0.00000	3
42	9.99485	.31073	0.00000	3
43	10.90882	.38168	0.00000	1
44	11.82279	.26983	0.00000	1
45	12.73676	.89318	0.00000	1
46	13.65073	.72653	0.00000	1
47	14.56470	.93916	0.00000	2
48	15.47867	1.01600	0.00000	3
49	16.39264	1.12285	0.00000	3
50	17.30661	1.20969	0.00000	3
51	18.22058	1.23653	0.00000	3
52	19.13455	1.41022	0.00000	3
53	20.04852	1.61193	0.00000	3
54	20.96249	1.81765	0.00000	3
55	21.87646	2.02137	0.00000	3
56	22.79043	2.22509	0.00000	3
57	23.70440	2.42881	0.00000	3
58	24.61837	2.63253	0.00000	3
59	25.53234	2.83625	0.00000	3
60	26.44631	3.03997	0.00000	3
61	27.36028	3.24369	0.00000	3
62	28.27425	3.44741	0.00000	3
63	29.18822	3.65113	0.00000	3
64	30.10219	3.85485	0.00000	3
65	31.01616	4.05857	0.00000	3
66	31.93013	4.26229	0.00000	3
67	32.84410	4.46601	0.00000	3
68	33.75807	4.66973	0.00000	3
69	34.67204	4.87345	0.00000	3
70	35.58601	5.07717	0.00000	3

CARD V. PART DEFINITION.																
NP 11 J1 12 J2 L1 L2 L3 L4 MT MN 13 J5 1R																
1	1	1	1	1	2	2	13	12	1	1	0	0	0	0	0	0
2	1	1	2	5	3	12	13	8	1	1	0	0	0	0	0	0
3	1	1	3	4	4	8	15	26	1	1	0	0	0	0	0	0
4	1	1	4	4	5	26	15	4	1	1	0	0	0	0	0	0
5	5	1	9	2	2	17	24	13	1	1	0	0	0	0	0	0
6	4	1	5	4	4	5	26	15	2	0	0	0	0	0	0	0
7	4	2	5	5	3	26	9	4	15	2	0	0	0	0	0	0
8	9	1	10	2	2	17	24	13	2	0	0	0	0	0	0	0
9	2	2	10	3	24	7	6	17	2	0	0	0	0	0	0	0
10	5	3	9	4	6	17	40	9	3	0	0	0	0	0	0	0
11	5	4	9	5	4	17	4	9	3	0	0	0	0	0	0	0
12	5	4	9	5	10	4	6	11	40	17	3	0	0	0	0	0
13	9	3	10	4	5	10	3	11	4	17	3	0	0	0	0	0
14	9	4	10	5	4	10	3	11	4	17	3	0	0	0	0	0
15	10	1	14	2	2	3	22	7	3	0	0	0	0	0	0	0
16	10	2	14	3	22	3	22	7	3	0	0	0	0	0	0	0
17	10	3	14	4	20	3	32	11	3	0	0	0	0	0	0	0
18	10	4	14	5	32	3	4	11	3	0	0	0	0	0	0	0
19	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

CARD VI. SECTION LOCATION.

Z - 0.050				
Z - 0.000				
	X	Y	Z	Y
71	1.0000	0.0000	2.0000	1
72	1.5000	0.0000	2.0000	1
73	1.8000	0.0000	2.0000	1
74	1.75173	0.0000	2.0000	1
75	2.30232	0.0000	2.0000	1
76	3.03834	0.0000	2.0000	1
77	3.21362	0.0000	2.0000	1
78	4.57225	0.0000	2.0000	1
79	5.50000	0.0000	2.0000	1
80	7.37500	0.0000	2.0000	1
81	8.26000	0.0000	2.0000	1
82	9.12500	0.0000	2.0000	1
83	10.00000	0.0000	2.0000	1
84	10.00000	0.0000	2.0000	1
85	10.0000	0.0000	2.0000	1
86	10.0000	0.0000	2.0000	1
87	10.0000	0.0000	2.0000	1
88	10.0000	0.0000	2.0000	1
89	10.0000	0.0000	2.0000	1
90	10.0000	0.0000	2.0000	1
91	10.0000	0.0000	2.0000	1
92	10.0000	0.0000	2.0000	1
93	10.0000	0.0000	2.0000	1
94	10.0000	0.0000	2.0000	1
95	10.0000	0.0000	2.0000	1
96	10.0000	0.0000	2.0000	1
97	10.0000	0.0000	2.0000	1
98	10.0000	0.0000	2.0000	1
99	10.0000	0.0000	2.0000	1
100	10.0000	0.0000	2.0000	1
101	10.0000	0.0000	2.0000	1

312	1.59774	.71773	8.00000	1		
313	2.00822	.84425	8.00000	2		
314	2.50192	.90190	8.00000	2		
315	3.10773	.96017	8.00000	2		
316	4.51166	.91141	8.00000	2		
317	5.31552	.87144	8.00000	2		
318	6.13441	.84779	8.00000	2		
319	7.25294	.82188	8.00000	3		
320	8.16691	.80493	8.00000	3		
321	9.08088	.78798	8.00000	3		
322	9.99485	.77103	8.00000	3		
323	1.10059	.75408	8.00000	1		
324	1.59175	.73713	8.00000	1		
325	1.80292	.72018	8.00000	1		
326	1.91388	.70323	8.00000	1		
327	2.11222	.68628	8.00000	1		
328	2.35352	.66933	8.00000	1		
329	2.62541	.65238	8.00000	1		
330	4.19730	.63543	8.00000	3		
331	5.16353	.61848	8.00000	3		
332	6.17953	.60153	8.00000	3		
333	7.00101	.58458	8.00000	3		
334	7.96477	.56763	8.00000	3		
335	8.85633	.55068	8.00000	3		
336	9.74489	.53373	8.00000	3		
337	1.00010	.51678	8.00000	1		
338	1.54616	.49983	8.00000	1		
339	1.80219	.48288	8.00000	1		
340	1.91703	.46593	8.00000	1		
341	2.00544	.44898	8.00000	2		
342	2.75437	.43203	8.00000	3		
343	3.42331	.41508	8.00000	3		
344	4.11224	.39813	8.00000	3		
345	4.80118	.38118	8.00000	3		
346	5.70107	.36423	8.00000	3		
347	6.55363	.34728	8.00000	3		
348	7.45304	.33033	8.00000	3		
349	8.16452	.31338	8.00000	3		
350	9.00000	.29643	8.00000	3		
1	1	16	71	72	85	1
2	2	17	16	73	86	1
3	3	18	17	74	87	1
4	4	19	18	75	88	1
5	5	20	19	76	89	1
6	6	21	20	77	90	1
7	7	22	21	78	91	1
8	8	23	22	79	92	1
9	9	24	23	80	93	2
10	10	25	24	81	94	1
11	11	26	25	82	95	1
12	12	27	26	83	96	1
13	13	28	27	84	97	1
14	14	29	28	85	98	1
15	15	30	29	86	99	2
16	16	31	30	87	100	2
17	17	32	31	88	101	2
18	18	33	32	89	102	2
19	19	34	33	90	103	2
20	20	35	34	91	104	2
21	21	36	35	92	105	2
22	22	37	36	93	106	2
23	23	38	37	94	107	2
24	24	39	38	95	108	2
25	25	40	39	96	109	2
26	26	41	40	97	110	2
27	27	42	41	98	111	2
28	28	43	42	99	112	2
29	29	44	43	100	113	2
30	30	45	44	101	114	2
31	31	46	45	102	115	2
32	32	47	46	103	116	2
33	33	48	47	104	117	2
34	34	49	48	105	118	2
35	35	50	49	106	119	2
36	36	51	50	107	120	2
37	37	52	51	108	121	2
38	38	53	52	109	122	2
39	39	54	53	110	123	2
40	40	55	54	111	124	2
41	41	56	55	112	125	2
42	42	57	56	113	126	2
43	43	58	57	114	127	2
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45	45	60	59	116	129	2
46	46	61	60	117	130	2
47	47	62	61	118	131	2
48	48	63	62	119	132	2
49	49	64	63	120	133	2
50	50	65	64	121	134	2
51	51	66	65	122	135	2
52	52	67	66	123	136	2
53	53	68	67	124	137	2
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55	55	70	69	126	139	2
56	56	71	70	127	140	2
57	57	72	71	128	141	2
58	58	73	72	129	142	2
59	59	74	73	130	143	2
60	60	75	74	131	144	2
61	61	76	75	132	145	2
62	62	77	76	133	146	2
63	63	78	77	134	147	2
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65	65	80	79	136	149	2
66	66	81	80	137	150	2
67	67	82	81	138	151	2
68	68	83	82	139	152	2
69	69	84	83	140	153	2
70	70	85	84	141	154	2
71	71	86	85	142	155	2
72	72	87	86	143	156	2
73	73	88	87	144	157	2
74	74	89	88	145	158	2
75	75	90	89	146	159	2
76	76	91	90	147	160	2
77	77	92	91	148	161	2
78	78	93	92	149	162	2
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87	87	102	101	158	171	2
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90	90	105	104	161	174	2
91	91	106	105	162	175	2
92	92	107	106	163	176	2
93	93	108	107	164	177	2
94	94	109	108	165	178	2
95	95	110	109	166	179	2
96	96	111	110	167	180	2
97	97	112	111	168	181	2
98	98	113	112	169	182	2
99	99	114	113	170	183	2
100	100	115	114	171	184	2
101	101	116	115	172	185	2
102	102	117	116	173	186	2
103	103	118	117	174	187	2
104	104	119	118	175	188	2
105	105	120	119	176	189	2
106	106	121	120	177	190	2
107	107	122	121	178	191	2
108	108	123	122	179	192	2
109	109	124	123	180	193	2
110	110	125	124	181	194	2
111	111	126	125	182	195	2
112	112	127	126	183	196	2
113	113	128	127	184	197	2
114	114	129	128	185	198	2
115	115	130	129	186	199	2
116	116	131	130	187	200	2
117	117	132	131	188	201	2
118	118	133	132	189	202	2
119	119	134	133	190	203	2
120	120	135	134	191	204	2
121	121	136	135	192	205	2
122	122	137	136	193	206	2
123	123	138	137	194	207	2
124	124	139	138	195	208	2
125	125	140	139	196	209	2
126	126	141	140	197	210	2
127	127	142	141	198	211	2
128	128	143	142	199	212	2
129	129	144	143	200	213	2
130	130	145	144	201	214	2
131	131	146	145	202	215	2
132	132	147	146	203	216	2
133	133	148	147	204	217	2
134	134	149	148	205	218	2
135	135	150	149	206	219	2
136	136	151	150	207	220	2
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138	138	153	152	209	222	2
139	139	154	153	210	223	2
140	140	155	154	211	224	2
141	141	156	155	212	225	2
142	142	157	156	213	226	2
143	143	158	157	214	227	2
144	144	159	158	215	228	2
145	145	160	159	216	229	2
146	146	161	160	217	230	2
147	147	162	161	218	231	2
148	148	163	162	219	232	2
149	149	164	163	220	233	2
150	150	165	164	221	234	2
151	151	166	165	222	235	2
152	152	167	166	223	236	2
153	153	168	167	224	237	2
154	154	169	168	225	238	2
155	155	170	169	226	239	2
156	156	171	170	227	240	2
157	157	172	171	228	241	2
158	158	173	172	229	242	2
159	159	174	173	230	243	2
160	160	175	174	231	244	2
161	161	176	175	232	245	2
162	162	177	176	233	246	2
163	163	178	177	234	247	2
164	164	179	178	235	248	2
165	165	180	179	236	249	2
166	166	181	180	237	250	2
167	167	182	181	238	251	2
168	168	183	182	239	252	2
169	169	184	183	240	253	2
170	170	185	184	241	254	2
171	171	186	185	242	255	2
172	172	187	186	243	256	2
173	173	188	187	244	257	2
174	174	189	188	245	258	2
175	175	190	189	246	259	2
176	176	191	190	247	260	2
177	177	192	191	248	261	2
178	178	193	192	249	262	2
179	179	194	193	250	263	2
180	180	195	194	251	264	2
181	181	196	195	252	265	2
182	182	197	196			

94	231	232	246	245	301	302	316	315	2
95	232	233	247	246	302	303	317	316	2
96	233	234	248	247	303	304	318	317	2
97	239	240	254	253	307	310	324	323	1
98	240	241	255	254	310	311	325	324	1
99	241	242	256	255	311	312	326	325	1
100	242	243	257	256	312	313	327	326	2
101	253	254	268	267	323	324	338	337	1
102	254	255	269	268	324	325	339	338	1
103	255	256	270	269	325	326	340	339	1
104	256	257	271	270	326	327	341	340	2
105	10	11	25	24	80	81	95	94	3
106	11	12	26	25	81	82	96	95	3
107	12	13	27	26	82	83	97	96	3
108	13	14	28	27	83	84	98	97	3
109	24	25	39	38	94	95	109	108	3
110	25	26	40	39	95	96	110	109	3
111	26	27	41	40	96	97	111	110	3
112	27	28	42	41	97	98	112	111	3
113	33	34	48	47	103	104	118	117	3
114	34	35	49	48	104	105	119	118	3
115	35	36	50	49	105	106	120	119	3
116	36	37	51	50	106	107	121	120	3
117	37	38	52	51	107	108	122	121	3
118	38	39	53	52	108	109	123	122	3
119	39	40	54	53	109	110	124	123	3
120	40	41	55	54	110	111	125	124	3
121	41	42	56	55	111	112	126	125	3
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15	103	117	187	173	1				
16	117	131	201	187	1				
17	150	164	234	220	1				

18	174	175	243	244	1
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21	177	176	246	247	1
22	178	177	247	248	1
23	173	187	257	263	1
24	187	201	271	257	1
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33	24	30	108	98	1
34	94	108	178	164	1
35	164	178	248	234	1
36	234	248	318	304	1

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